

Capitolo 8

Argomenti e implicazioni per i *Principles and Standards*

#10**Reazione del lettore**

Lo sviluppo del capitolo 8 verrà basato, in parte, sulle risposte e le reazioni raccolte nel corso dell'anno scolastico 1998-99.

Lo scopo sarà quello di metter in evidenza i problemi nell'attuazione delle idee di *Principles and Standards* e determinare linee guida. Ti chiediamo di contribuire a questo processo rispondendo alle seguenti domande:

- **Per ognuno dei seguenti livelli di programmazione didattica della matematica, quali *argomenti* è necessario discutere ulteriormente?**
 - (a) a livello di classe
 - (b) a livello di scuola
 - (c) a livello di provincia o di Stato
 - (d) a livello nazionale
- **Quali *linee guida* possono essere proposte in ognuna delle seguenti aree?**
 - (a) sviluppo di materiali didattici
 - (b) preparazione matematica degli insegnanti
 - (c) sviluppo della professionalità docente
 - (d) amministrazione scolastica
 - (e) istruzione superiore

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